

## Multitask group Lasso for Genome Wide association Studies in diverse populations

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Genome-Wide Association Studies, or GWAS, aim at finding Single Nucleotide Polymorphisms (SNPs) that are associated with a phenotype of interest. GWAS are known to suffer from the large dimensionality of the data with respect to the number of available samples. Other limiting factors include the dependency between SNPs, due to linkage disequilibrium (LD), and the need to account for population structure, that is to say, confounding due to genetic ancestry.

We propose an efficient approach for the multivariate analysis of multi-population GWAS data based on a multitask group Lasso formulation. Each task corresponds to a subpopulation of the data, and each group to an LD-block. This formulation alleviates the curse of dimensionality, and makes it possible to identify disease LD-blocks shared across populations/tasks, as well as some that are specific to one population/task. In addition, we use stability selection to increase the robustness of our approach. Finally, gap safe screening rules speed up computations enough that our method can run at a genome-wide scale.

To our knowledge, this is the first framework for GWAS on diverse populations combining feature selection at the LD-groups level, a multitask approach to address population structure, stability selection, and safe screening rules. We show that our approach outperforms state-of-the-art methods on both a simulated and a real-world cancer datasets.

*Keywords:* Genome Wide Association Studies, Feature selection, Multitask group Lasso, Stability selection, Safe screening rules

### 1. Introduction

Over the last 15 years, Genome-Wide Association Studies (GWAS) have become one of the most prevalent methods to identify regions of the genome associated with complex phenotypic traits, and in particular complex diseases in humans.<sup>1</sup> One of the major concerns in GWAS is population stratification, which arises when allele frequency differences between cases and controls are due to differences in genetic ancestry rather than to association with the phenotype. Many correction methods have been proposed to adjust the inflation of associations in diverse populations, including methods based on principal components analysis or on linear mixed models.<sup>2</sup> However, it is possible that these techniques lead to overcorrection, in particular by

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masking population-specific disease loci.

An additional issue in GWAS is Linkage Disequilibrium (LD), which manifests as correlation between adjacent Single Nucleotide Polymorphisms (SNPs), creating statistical dependence between those markers and reducing statistical power.<sup>3</sup> Combining strongly correlated SNPs into blocks, that is to say, groups of adjacent and correlated SNPs, and modeling the association signal over an entire region, is one way to address this limitation.

Classical approaches for GWAS are based on single-marker analyses, testing for association between each SNP and the phenotype independently. This may prevent the detection of effects that are due to SNPs acting additively, leading many authors to favor fitting a linear model to all SNPs jointly.<sup>4</sup> Penalized regression approaches, such as the Lasso, which uses an  $\ell_1$ -norm regularization to shrink some coefficients of the model to zero, effectively removing them from the model, are particularly suited to this task.

Additional regularizers can be used to enforce additional prior hypotheses on the coefficients of such a linear model. Among them, the group Lasso<sup>3,5</sup> ensures sparsity at the level of pre-defined groups of features, and the multitask Lasso<sup>6,7</sup> fits models on related tasks jointly, encouraging similar sparsity patterns across all tasks.

In this work, we propose to combine both approaches into a multitask group Lasso framework, in which groups correspond to pre-defined LD patterns, and each task corresponds to a subpopulation, therefore simultaneously addressing the limitations of single-marker analyses and the issues of both LD and population structure.

In addition, we draw on the stability selection framework<sup>8</sup> to improve the stability of the results, that is to say, their robustness to small perturbations in the input data, such as the removal of a few samples. Indeed, because the number of SNPs is typically much larger than that of samples, penalized regression approaches tend to select different sets of SNPs when presented with slightly different subsets of the same data, which severely limits their interpretability.

Finally, we use the recently proposed gap safe screening rules proposed by E. Ndiaye et al.<sup>9</sup> to improve computational complexity, and scale our approach to about one million SNPs.

In what follows, we present our proposed approach in detail, place it in the context of existing work, and evaluate it on both a simulated data set and a real-world cancer GWAS data set.

## 2. Methods

Our proposed approach, MuGLasso, follows four steps, which we detail in this Section. First, we assign each sample to a genetic population, hence forming different but related tasks (Section 2.1). Second, we create LD-groups from correlations between SNPs, so as to perform feature selection at the level of groups rather than individual SNPs (Section 2.2). Third, we jointly fit one regularized model per task, using an  $\ell_{2,1}$  penalty that enforces sparsity at the level of LD-groups (Section 2.3). Finally, we use stability selection to improve the robustness of the solution (Section 2.4).

## 2.1. *Population stratification*

Population structure, whereby the data is made of subsets of individuals that differ systematically both in genetic ancestry and in the phenotype under investigation, is a major confounding factor in GWAS. Indeed, it leads to detecting allele frequency differences in cases and controls that correspond to differences in ancestry, instead of a more direct association between genotype and phenotype. Several approaches have been developed to adjust for population structure.

Among them, a large number of methods rely on Principal Component Analysis (PCA),<sup>10-12</sup> and consist of including top Principal Components (PCs) of the genotypes as covariates in regression models. In addition, linear mixed models<sup>13</sup> can be used to model the phenotype as a combination of fixed and random effects, with the covariance of the latter being computed from a genetic similarity matrix. Although they often outperform PCA-based methods, the mixed model approaches tend to be more computationally demanding. Both approaches are similar in that regressing out principal components can be seen as approximation of a linear mixed model.<sup>2</sup>

However, these techniques may lead to ignoring population-specific SNPs, which is why we propose a multitask approach that can identify disease loci that are either population-specific or shared between populations. We therefore form tasks by separating the data into subpopulations, identified as clusters (using k-means clustering) on the projection of the genotypes on their top PCs.

## 2.2. *Linkage disequilibrium groups*

Linkage disequilibrium (LD) is the non-random association of alleles of at least two loci.<sup>14</sup> LD can be leveraged to form groups of correlated SNPs. Grouping SNPs helps to alleviate the curse of dimensionality in GWAS by reducing the number of testing possibilities. This can be achieved by combining p-values within a group of correlated SNPs<sup>15</sup>, or through the use of penalized regression approaches that perform feature selection at the level of groups, rather than at the level of individual SNPs.<sup>3</sup> The latter has the advantage over individual statistical testing of modeling the additive effects of multiple genetic markers simultaneously.

### 2.2.1. *Adjacency-constrained hierarchical clustering*

In many species, including humans,<sup>16</sup> LD is known to be correlated to the physical distance between SNPs. Hence, genomes can be clustered in LD blocks of strongly correlated adjacent SNPs, called in this paper LD-groups. Such LD-groups can be obtained using adjacency-constrained hierarchical agglomerative clustering,<sup>3</sup> in which only physically adjacent clusters can be merged.

### 2.2.2. *LD-groups across populations*

Because LD patterns may be influenced by genetic ancestry,<sup>17</sup> we perform LD-groups partitioning for each population separately. We then combine those LD-groups into common shared LD-groups. More specifically, the set of coordinates of the boundaries of the shared LD-groups

is obtained as the union of the sets of coordinates of the boundaries of the LD-groups for each population. This procedure is described in Supplementary Figure B1.

### 2.3. Multitask group Lasso

#### 2.3.1. General framework and problem formulation

We use a penalized regression approach to fit a multivariate linear model between the phenotype and the SNPs, with a regularization term that ensures that (1) the solution is sparse at the level of LD-groups and (2) the regression coefficients are smoothed within groups and across tasks. Such an approach provides shared LD-groups associated with the phenotype across all tasks, and allows for some LD-groups to be specific to each task.

**Problem formulation** Given a set of  $p$  SNPs measured for  $n$  samples, we split the  $n$  samples in  $T$  subpopulations/tasks, each of size  $n_t$  for  $t = 1, \dots, T$ , and the  $p$  SNPs in  $G$  LD-groups, each of size  $p_g$  for  $g = 1, \dots, G$ . For each population  $t$ , we denote by  $\mathbf{x}_m^{(t)}$  the  $p$ -dimensional vectors of SNPs of the  $m$ -th sample in the population ( $m = 1, \dots, n_t$ ), and by  $y_m^{(t)}$  its phenotype. We then formulate the following optimization problem:

$$\min_{B \in \mathbb{R}^{p \times T}} \frac{1}{n} \sum_{t=1}^T \sum_{m=1}^{n_t} \mathcal{L} \left( y_m^{(t)}, \sum_{j=1}^p \beta_j^{(t)} x_{mj}^{(t)} \right) + \lambda \sum_{g=1}^G \sqrt{p_g} \left\| B^{(g)} \right\|_F, \quad (1)$$

where  $\beta^{(t)} \in \mathbb{R}^p$  is the vector of regression coefficients specific to task  $t$ :  $\beta^{(t)} = (B_{1t}, \dots, B_{pt})$ ,  $\mathcal{L}$  is the quadratic loss if the phenotype is quantitative ( $y \in \mathbb{R}$ ) and the logistic loss if it is qualitative ( $y \in \{0, 1\}$ ),  $\|\cdot\|_F$  denotes the Frobenius norm, and  $B^{(g)}$  is a  $p_g \times T$  matrix containing the regression coefficients, across all tasks, for the SNPs of group  $g$ .

#### 2.3.2. Related work

**$\ell_{2,1}$ -norm regularization** Our approach is closely related to the group Lasso<sup>5</sup> and multitask Lasso,<sup>6</sup> which both make use of an  $\ell_{2,1}$ -norm regularization. More precisely, the group Lasso corresponds to a special case of Equation (1), with a single task ( $T = 1$ ), resulting in sparsity at the group levels. Using a group Lasso where the groups are defined based on LD blocks has been successfully applied to GWAS on up to 20 000 SNPs.<sup>3</sup> The multitask Lasso corresponds to a special case of Equation (1), with each group containing exactly one SNP. This formulation ties sparsity patterns across tasks and has been applied before to multi-population GWAS, although only a few thousand SNPs.<sup>7</sup>

The multitask group Lasso we propose can also be reformulated as an  $\ell_{2,1}$ -norm regularization problem, through the creation of a new dataset  $(\tilde{X}, \tilde{\mathbf{y}})$  where  $\tilde{X} \in \mathbb{R}^{n \times pT}$  is a block-diagonal matrix such that each of the  $T$  diagonal blocks corresponds to the SNP matrix  $X^{(t)} \in \mathbb{R}^{n_t \times p}$  for task  $t$ , and  $\tilde{\mathbf{y}}$  is a  $n$ -dimensional vector obtained by stacking the phenotype vectors for each task. Equation (1) can then be rewritten as:

$$\min_{\mathbf{b} \in \mathbb{R}^{pT}} \frac{1}{n} \sum_{i=1}^n \mathcal{L} \left( \tilde{y}_i, \sum_{k=1}^{pT} b_k \tilde{x}_{ik} \right) + \lambda \sum_{g=1}^G \sqrt{p_g} \left\| \mathbf{b}^{(g)} \right\|_2, \quad (2)$$

with  $\mathbf{b}^{(g)} \in \mathbb{R}^{p_g T}$  the regression coefficients corresponding to all SNPs of group ( $g$ ) for all tasks. In essence, this is a group Lasso with  $G$  groups each containing  $T$  copies (one per task) of the  $p_g$  features of SNP group  $g$ . Thus  $B_{jt} = \mathbf{b}_{p(t-1)+j}$ .

**Other multitask group Lassos** Other authors have proposed variations on the idea of a multitask group Lasso before. Several publications<sup>18,19</sup> add a second regularization term to our formulation, increasing within-group or across-task sparsity. Unfortunately, this dramatically increases computational time, and indeed none of these publications analyze genome-wide data sets. In addition, because interpretation will be done at the group level rather than at the SNP level, within-group sparsity is not necessarily desirable in this context.

Several authors have built on these propositions and add a third regularization term, either enforcing group-independent task sparsity<sup>20</sup> or overall sparsity (with an  $\ell_1$ -norm over all coefficients).<sup>21</sup> Again, the addition of these regularizers severely hinders the applicability of these methods at a genome-wide scale due to computational limitations.

Hence none of these methods is readily applicable to our setting. In addition, their stability has never been evaluated, even though it is an important criterion for the reliability and interpretability of the results (see Section 2.4).

### 2.3.3. Gap safe screening rules

To speed up the computation of the solution of Equation (2), we call upon gap safe screening rules,<sup>9</sup> which are used to efficiently identify features for which the regression coefficients will be zero and hence ignore them when solving the problem. Such screening rules have been proposed for a large number of popular regularized regressions,<sup>9</sup> including  $\ell_{2,1}$ -norm regularizations. In particular, Equation (2) can be solved using the `Gap_Safe_Rule` package<sup>a</sup>. We briefly summarize the idea underlying gap safe screening rules in Appendix B.3.

## 2.4. Stability selection

Unfortunately, in GWAS, penalized regression approaches often lack stability, that is to say, robustness to slight variations in the input dataset.<sup>22</sup> However, stability increases both the reliability of the results and the interpretability. To address this limitation, *stability selection*<sup>8,22</sup> consists of performing feature selection repeatedly on subsamples of the data and only retains the features most often selected. More specifically, given a subsample  $I \subset \{1, \dots, n\}$  of size  $\lfloor n/2 \rfloor$  of the data, we call  $\widehat{S}^\lambda(I)$  the set of features selected by the selection procedure of interest (for example, a Lasso), with hyperparameter  $\lambda$ , on this subsample of the data. For any feature  $j \in \{1, \dots, p\}$ , we call  $\widehat{\Pi}_j^\lambda$  the probability that feature  $j$  is selected on a random subsample of size  $\lfloor n/2 \rfloor$  of the data. This probability is determined, given  $m$  such random subsamples  $I_1, I_2, \dots, I_m$ , as the proportion of those subsamples for which the feature selection procedure selects feature  $j$ :  $\widehat{\Pi}_j^\lambda = \frac{1}{m} \sum_{k=1}^m \mathbf{1}_{j \in S^\lambda(I_k)}$ . Finally, given a threshold  $\frac{1}{2} < \pi_{\text{cutoff}} \leq 1$  (in this work, we used  $\pi_{\text{cutoff}} = 0.75$ ), the stable set of selected features is determined as  $\widehat{S}^{\text{stable}} = \{j : \max_{\lambda \in \Lambda} \widehat{\Pi}_j^\lambda \geq \pi_{\text{cutoff}}\}$ .

<sup>a</sup>[https://github.com/EugeneNdiaye/Gap\\_Safe\\_Rules](https://github.com/EugeneNdiaye/Gap_Safe_Rules)

### 3. Experiments

#### 3.1. Data

**Simulated data** Using GWASimulator,<sup>23</sup> we simulated GWAS data with realistic LD patterns from two populations (CEU : Utah residents with Northern and Western European ancestry and YRI: Yoruba in Ibadan, Nigeria) of the HapMap 3 data. We induced population structure by varying the case:control ratio within each subpopulation (CEU 1 100:900 and YRI 900:1 100), as well as by simulating population-specific disease loci. We simulated a total of 149 970 disease SNPs, 2 999 (resp 4 999) of which are specific to the CEU (resp. YRI) population (see Appendix A.1). The data contains 4 000 samples and 1 400 000 SNPs.

**DRIVE Breast Cancer OncoArray** The DRIVE OncoArray dataset (dbGap study accession phs001265/GRU) contains 28 281 individuals that were genotyped for 582 620 SNPs. 13 846 samples are cases and 14 435 are controls. More details are available in Appendix A.2.

#### 3.2. Preprocessing

**Quality control and imputation** We removed SNPs with a minor allele frequency lower than 5%, a p-value for Hardy-Weinberg Equilibrium in controls lower than 10%, or a missing genotyping rate larger than 10%. We removed duplicate SNPs and excluded samples with more than 10% of SNPs missing. We imputed missing genotypes in DRIVE using IMPUTE2.<sup>24</sup>

**LD pruning** We performed LD pruning using PLINK<sup>25</sup> with a LD cutoff of  $r^2 > 0.85$  and a window size of 50Mb, both to reduce the number of SNPs and to better capture population structure using PCA.<sup>26</sup> 1 000 000 SNPs remain in the simulated data and 313 237 in DRIVE.

**PCA and population structure** We used PLINK<sup>25</sup> to compute principal components of the genotypes. We thus identify two populations in the simulated data, matching the CEU and YRI populations (see Supplementary Figure C1a). In DRIVE, we identify two populations (see Supplementary Figure C1b), which we call POP1 (samples from the USA, Australia and Denmark) and POP2 (samples from the USA, Cameroon, Nigeria and Uganda).

**LD-groups choice** We obtain LD-groups for each of the PCA-based populations using adj-clust<sup>27</sup> and obtain shared LD-groups as described in Section 2.2.2. Table 1 shows the number of LD-groups obtained for each subpopulation and the final number of shared groups.

Table 1. For each subpopulation of both datasets (simulated and real), LD-groups number is given and the shared LD-groups number after combination

Data	Subpopulations	LD-groups number	Shared LD-groups number
Simulated data	CEU	25 281	35 792
	YRI	15 636	
DRIVE real data	POP1	8 152	17 782
	POP2	5 032	

### 3.3. Comparison partners

As a baseline, we use PLINK<sup>25</sup> to perform tests of association between each SNP and the phenotype, either using the top PCs as covariates (**Adjusted GWAS**), or treating each population separately (**Stratified GWAS**). We also compute a PCA-adjusted phenotype as the residuals of a regression between the top PCs and the phenotype. To evaluate the effects of grouping correlated SNPs and separating the populations in tasks, we compare MuGLasso to a Lasso (single task, no groups) on each population (**Stratified Lasso**) or on the adjusted phenotype (**Adjusted Lasso**), as well as a group Lasso (single task) on each population (**Stratified group Lasso**) or on the adjusted phenotype (**Adjusted group Lasso**).

For computational efficiency, we use bigLasso<sup>28</sup> for the Lasso, and Gap\_Safe\_Rule<sup>9</sup> for the group Lasso. For all methods, we set the regularization hyperparameter by cross-validation.

To compare these methods, we report runtime, ability to recover true causal SNPs (in the case of simulated data), and stability of the selection. To measure selection stability, we repeat the feature selection procedure on 10 subsamples of the data, and report the average Pearson’s correlation between all pairs of indicator vectors representing the selected features for each subsample (see Appendix B.4 for details).

## 4. Results

### 4.1. MuGLasso draws on both LD-groups and the multitask approach to recover disease SNPs

On the simulated data, we observe (Figure 1a) that MuGLasso is better than any other method at recovering the true disease SNPs. Performing feature selection at the level of LD-groups, rather than individual SNPs, improves performance. Indeed, the group Lassos and MuGLasso outperform the SNP-level Lassos. In addition, treating all samples simultaneously (as in MuGLasso or the adjusted approaches) also improves performance. This confirms our hypothesis that grouping features and using all samples simultaneously both alleviate the curse of dimensionality.

On DRIVE, MuGLasso recovers 1051 SNPs in addition to all SNPs from the adjusted GWAS. They point to 32 risk genes that cannot be identified by the classical GWAS; half of those have been identified in meta-GWAS that included our samples, and another 7 have been associated with breast cancer risk or growth in other studies (see Supplementary Table C1).

However, this increased ability to recover relevant SNPs comes with an increase in computational time (see Supplementary Figure C2 on simulated data and Figure 2a on DRIVE). However, the implementation is efficient enough to allow computations on  $10^6$  SNPs, even with the added cost of repeated subsampling to increase stability.

### 4.2. MuGLasso provides the most stable selection

Figures 1b (simulated data) and 2b (DRIVE) show the stability index of MuGLasso as a function of the number of subsamples. Increasing the number of subsamples increases the stability of the selection. We use 100 bootstrap samples in all subsequent experiments as it appears to be an acceptable trade-off between runtime and stability.

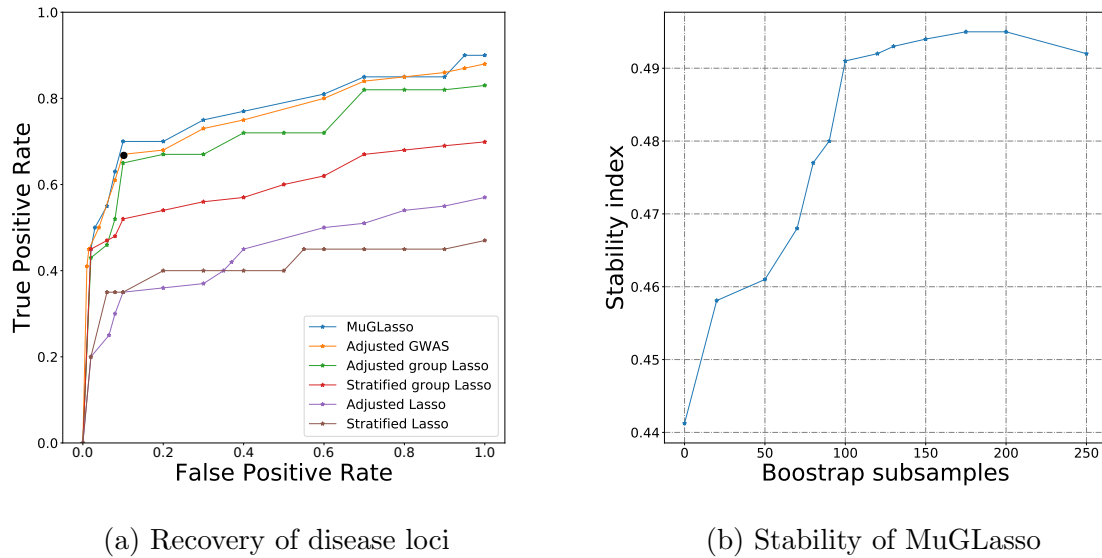


Fig. 1. On simulated data, ability of different methods to retrieve causal disease SNPs as a ROC plot (1a), and stability index of MuGLasso as a function of the number of bootstrap samples (1b). On the ROC plot, the black dot indicates the performance of the stratified GWAS at the Bonferonni-corrected significance threshold.

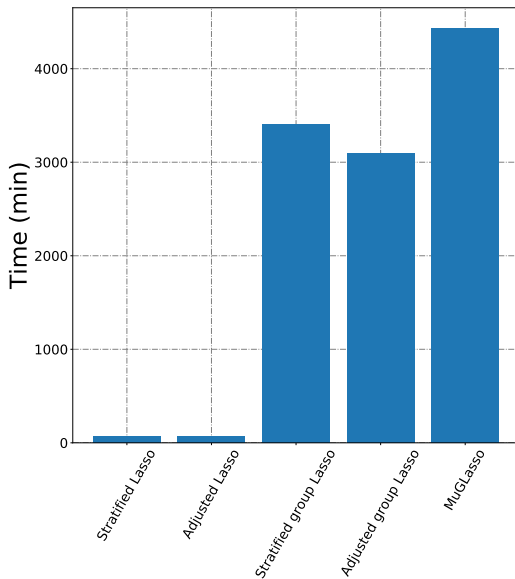
Tables 2 and 3 show the stability index of the different methods, on simulated data and DRIVE, respectively. We ran the adjusted GWAS once on the entire data set, as would usually be done, and therefore cannot report its stability. Our results again illustrate that stability selection does increase the stability of Lasso methods. We confirm this by running MuGLasso without stability selection as well as Adjusted group Lasso with stability selection on top. In both cases, the stability index increases when stability selection is used. In addition, we report the total number of selected SNPs and LD-groups. For methods that select individual SNPs, we obtain the number of selected LD-groups by considering that each selected SNP selects its entire LD-group. Our results illustrate that the improved stability of MuGLasso does not come at the expense of selecting more features. On the contrary, stability selection provides fewer SNPs/LD-groups with better stability.

#### 4.3. MuGLasso selects both task-specific and global LD-groups

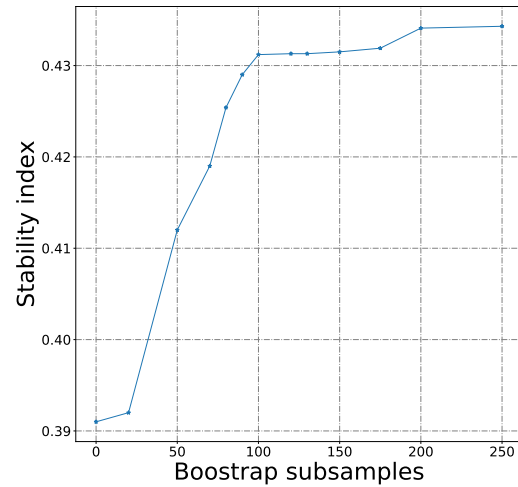
For both datasets, the LD-groups selected by MuGLasso are a mixture between population-specific LD-groups (identified as those with near-zero regression coefficients for one task) and LD-groups that are shared between both populations. Table 4 shows the number of LD-groups/SNPs in each of these categories for MuGLasso. By contrast, the adjusted approaches do not provide population-specific LD-groups or SNPs.

Finally, we report on Figure 3 the precision and recall of MuGLasso and the stratified approaches on the population-specific SNPs. MuGLasso outperforms all other approaches in both precision and recall.





(a) Runtimes of the Lasso approaches



(b) Stability of MuGLasso

Fig. 2. On DRIVE, runtimes of the different Lasso approaches (2a) and stability index of MuGLasso as a function of the number of bootstrap samples (2b).

Table 2. Stability index and number of selected features for different methods, on simulated data

Methods	Number of selected LD-groups	Number of selected SNPs	Stability index	Selection level
MuGLasso	5 623	155 312	0.4912	LD-groups
MuGLasso without stab sel	6 124	161 221	0.4412	LD-groups
Adjusted group Lasso + stab sel	6 054	162 104	0.4134	LD-groups
Adjusted group Lasso	6 347	167 204	0.3714	LD-groups
Stratified group Lasso	4 836	154 732	0.3398	LD-groups
Adjusted Lasso	5 379	158 856	0.2368	Single-SNP
Stratified Lasso	5 704	168 158	0.1742	Single-SNP
Adjusted GWAS	5 063	141 340	-	Single-SNP

## 5. Discussion and Conclusions

We presented MuGLasso, an efficient approach for detecting disease loci in GWAS data from diverse populations. Our approach is based on a multitask framework, where input tasks correspond to subpopulations, and feature selection is performed at the level of LD-groups. Assigning samples from PCA-identified populations to different tasks addresses the issue of population stratification, and retains the flexibility of identifying population-specific disease loci. Treating all samples together, by contrast with stratified approaches, alleviates the curse of dimensionality. Ensuring sparsity at the level of LD-groups addresses the high correlation between nearby SNPs and also alleviates the curse of dimensionality. Although more time-

Table 3. Stability index and number of selected features for different methods, on DRIVE

Methods	Number of selected LD-groups	Number of selected SNPs	Stability index	Selection level
MuGLasso	62	1 357	0.4312	LD-groups
MuGLasso without stab sel	72	1 524	0.3911	LD-groups
Adjusted group Lasso + stab sel	59	1 293	0.3234	LD-groups
Adjusted group Lasso	68	1 466	0.2613	LD-groups
Stratified group Lasso	58	1 119	0.2498	LD-groups
Adjusted Lasso	41	874	0.2068	Single-SNP
Stratified Lasso	38	789	0.1581	Single-SNP
Adjusted GWAS	16	306	-	Single-SNP

Table 4. For MuGLasso, number of selected LD-groups/SNPs, across and per population

Data	Population	Number of selected LD-groups (and SNPs)
Simulated data	CEU	95 (2 418 SNPs)
	YRI	103 (3 081 SNPs)
	shared (CEU and YRI)	5 227 (149 813 SNPs)
DRIVE	POP1	6 (148 SNPs)
	POP2	2 (43 SNPs)
	shared (POP1 and POP2)	54 (1166 SNPs)

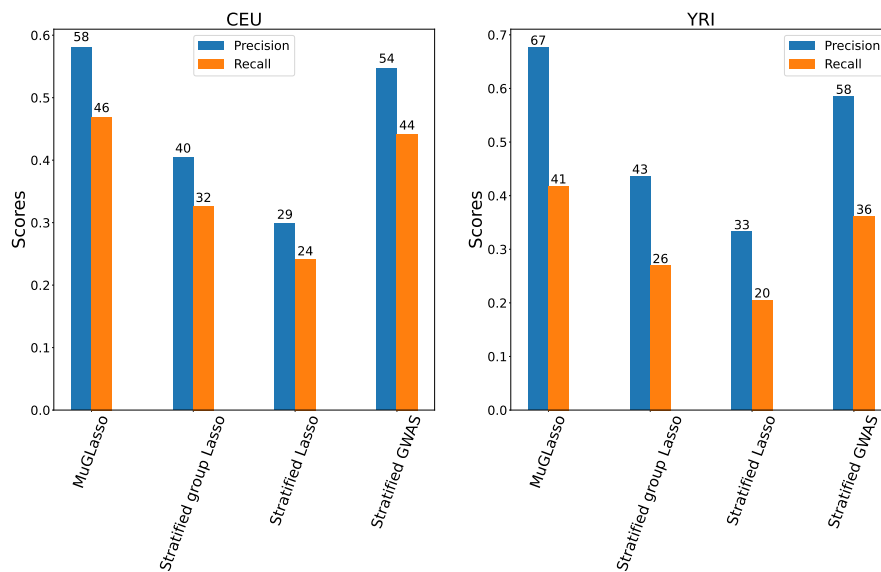


Fig. 3. For simulated data, precision and recall of MuGLasso and the stratified approaches on the populations-specific SNPs

consuming than a classical GWAS, our implementation is computationally efficient enough to scale to the analysis of entire GWAS data sets of about one million SNPs.

On simulated data, MuGLasso outperforms state-of-the-art approaches in its ability to recover disease loci. This also holds for population-specific SNPs; hence performance is not driven solely by the ability to recover disease loci that are common to all populations. In ad-

dition, MuGLasso is the most stable of all evaluated method, which increases interpretability.

Finally, although we presented MuGLasso in the context of admixed populations, our tool could be used in other multitask settings. In particular, tasks can stem from related phenotypes<sup>18</sup> or from different studies pertaining to the same trait, in a meta-analysis approach.<sup>19</sup> Groups could also be defined according to different prior biological knowledge, for example based on functional units such as genes, in the spirit of gene-set analyses of GWAS data. In addition, although we only presented results on case-control studies with two populations, the method directly applies to quantitative phenotypes and any number of tasks.

An important outcome of our study is that, although we have not included in MuGLasso a regularization term that would enforce sparsity at the level of tasks as in Li et al. (2020),<sup>21</sup> we still obtain task-specific groups. Including such an additional term in Equation (1) would perhaps improve the already state-of-the-art task-specific precision and recall of MuGLasso, but this would unfortunately come at the expense of a notable increase in computational time, if only because of the cross-validation needed to set the value of a second hyperparameter.

An in-depth biological analysis of the loci identified by MuGLasso on DRIVE would illustrate the biological relevance of our method, but is out of the scope of this methodological paper.

In the future, we are looking forward to making use of the post-inference selection framework for group-sparse linear models<sup>29</sup> to provide p-values for the selected loci. As of now, it is unclear how to apply these ideas to case-control studies in a computationally efficient manner.

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**Supplementary Materials and code** Supplementary materials are available online at <https://www.biorxiv.org/content/10.1101/2021.08.02.454499>. Code is available at [https://github.com/asmanouira/MuGLasso\\_GWAS](https://github.com/asmanouira/MuGLasso_GWAS).

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